

*First Measurements of the Polarized Spin Density
Matrix Elements along with a Partial Wave Analysis
for $\gamma p \rightarrow p\omega$ using CLAS at Jefferson Lab*

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Thesis Defense

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OUTLINE

- 1 INTRODUCTION
- 2 DATA SELECTION
- 3 SPIN DENSITY MATRIX ELEMENTS
- 4 PARTIAL WAVE ANALYSIS
- 5 SUMMARY

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QUANTUM CHROMODYNAMICS

- What is happening inside of a nucleon?
- Nucleons are made of quarks and gluons
- QCD is the theory of how quarks and gluons interact
- The *charge* term for QCD is called color charge and comes in three forms: red, green, and blue
- Quarks and gluons carry color charge, as well as electromagnetic charge
- How can we study what is happening inside of a nucleon?

BARYON SPECTROSCOPY

- Photons can be used to probe nucleons
- A photon strikes a nucleon, which absorbs the photon and enters an excited state briefly before returning to the ground state
- It returns to the ground state by emitting baryons and mesons
- The spectrum of excited nucleon states, or resonances, is discrete
- Excited states are characterized by
 - Total Angular Momentum, J
 - Parity, P
 - Mass
 - Width/Lifetime

RESONANCES

- The PDG currently lists 15 resonances whose presence is likely
- There are an additional 11 states that have been detected, but not confirmed
- Theory predicts more than twice as many states: *missing baryon problem*
- Simplify by looking at a single decay product
- We will attempt to probe the resonances by looking at one particular decay product, the ω meson

THE ω MESON

- Spin-1, or vector, meson
- Rest mass = 782.59 ± 0.11 MeV
- Width = 8.49 MeV $\rightarrow$ Lifetime = 7.75×10^{-23} s
- Charge = 0
- Isospin = 0
 - Can only couple to N^* states, not Δ^* s
- Branching Ratios:
 - $\pi^+ \pi^- \pi^0 \rightarrow 89.1\%$
 - $\pi^0 \gamma \rightarrow 8.92\%$
 - $\pi^+ \pi^- \rightarrow 1.70\%$
 - All others $\rightarrow 0.28\%$
- We will be looking at the $\pi^+ \pi^- \pi^0$ decay channel

METHODOLOGY

- To perform a complete analysis of ω photoproduction, the elements of its spin density matrix (SDM) must be measured
- The method used to extract the SDM elements (SDMEs) is to run a unbinned expanded maximum likelihood fits of the four vectors using partial wave amplitudes
- Use the parameters from that fit to calculate the SDMEs
- The formalism has been developed over the last few years to deal with polarized photons
- Determine which resonances are important for ω production using partial wave analysis
- Knowledge of the SDM will help constrain the partial wave analysis
- Adding in photon polarization increases analyzing power for PWA

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JEFFERSON LAB

- The data for this analysis was taken at Jefferson Lab in Newport News, VA, using the CEBAF Large Acceptance Spectrometer (CLAS)
- Jefferson Lab utilized a continuous electron beam, with energies up to 6 GeV, that is converted to a photon beam via bremsstrahlung reactions for the experiments analyzed here
- The photon beam can have linear or circular polarization or be unpolarized
- The experiments analyzed, g1c and g8b, used an unpolarized liquid hydrogen target with a circularly/linearly polarized photon beam

THE g1C DATASET

- Collected in October and November of 1999
- 4.5 billion triggers
- Unpolarized target
- Three different beam energies:
 - 3.115 GeV - No polarization values recorded (not analyzed)
 - 2.897 GeV - Incomplete normalization values
 - 2.445 GeV
- Circularly polarized photons
- Degree of circular polarization determined from Maximon and Olson relation

$$\zeta_c = \frac{k(\epsilon_{beam} + \frac{1}{3}\epsilon_{recoil})\zeta_{beam}}{\epsilon_{beam}^2 + \epsilon_{recoil}^2 - \frac{2}{3}\epsilon_{beam}\epsilon_{recoil}}$$

THE G8B DATASET

- Collected in July and August of 2005
- 10.5 billion triggers
- Unpolarized target
- Linearly polarized photons (coherent bremsstrahlung)
- Five different coherent edge settings from 1.3 GeV - 2.1 GeV
- Polarization in PARA and PERP directions
- Degree of linear polarization determined from tables based on photon energy and the instantaneous coherent edge

EVENT SELECTION

- Require detection of p , π^+ , and π^-
- Apply ELoss, tagger and momentum corrections
- Require events meet the requirements:
 - $|\vec{p}_p| \geq 350$ MeV
 - $0 \leq \text{missing mass} \leq 450$ MeV
 - Missing mass off proton within 25 MeV of ω mass, 782 MeV
 - Confidence Level from 1C kinematic fit to $\gamma p \rightarrow p\pi^+\pi^-(\pi^0) \geq 10\%$
 - Pass PID, fiducial volume, and TOF paddle cuts
 - $\cos\theta_{CM}^{\pi^0} > 0.99$
- Event-based Q-values to weight signal and background events
- g1c: 650,000 ω events in $1720 \leq \sqrt{s} \leq 2470$ MeV
- g8b: 2,900,000 ω events in $1720 \leq \sqrt{s} \leq 2210$ MeV

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SPIN DENSITY MATRIX

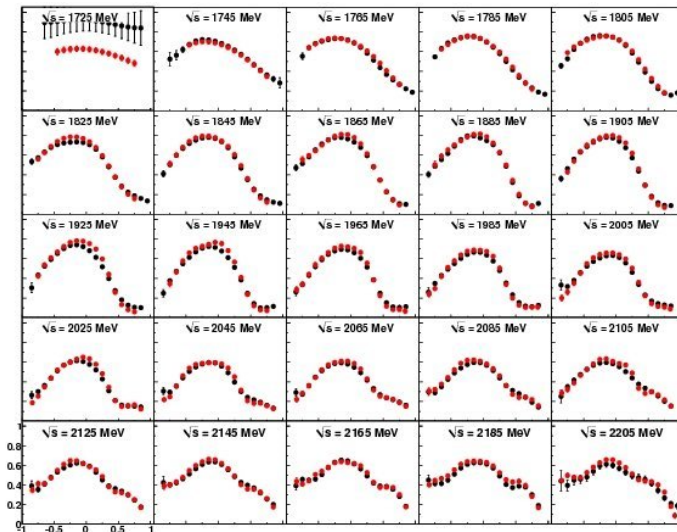
- The spin density matrix of a vector meson photoproduced from an unpolarized target can be thought of as the sum of four 3x3 Hermitian matrices
 - ρ^0 - Any photon polarization
 - ρ^{1-2} - Linear photon polarization
 - ρ^3 - Circular photon polarization
- Each of these matrices contains 9 complex values, but the properties of being a Hermitian matrix and parity reduce that number to 5 real values for each matrix
- All 5 values cannot be measured for each matrix
- The next slide shows each matrix, the measurable elements are underlined

SPIN DENSITY MATRIX

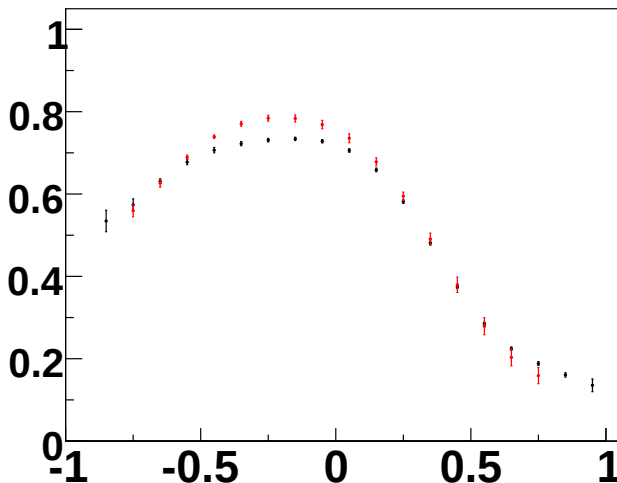
$$\begin{aligned}
\rho^0 &= \begin{pmatrix} \frac{1}{2}(1 - \rho_{00}^0) & \frac{\text{Re}\{\rho_{10}^0\} + i * \text{Im}\{\rho_{10}^0\}}{\rho_{00}^0} & \frac{\text{Re}\{\rho_{1-1}^0\}}{\frac{1}{2}(1 - \rho_{00}^0)} \\ \cdot & \cdot & \frac{-\text{Re}\{\rho_{10}^0\} + i * \text{Im}\{\rho_{10}^0\}}{\frac{1}{2}(1 - \rho_{00}^0)} \end{pmatrix} \\
\rho^1 &= \begin{pmatrix} \frac{\rho_{11}^1}{\rho_{00}^1} & \frac{\text{Re}\{\rho_{10}^1\} + i * \text{Im}\{\rho_{10}^1\}}{\rho_{00}^1} & \frac{\text{Re}\{\rho_{1-1}^1\}}{\rho_{11}^1} \\ \cdot & \cdot & \frac{-\text{Re}\{\rho_{10}^1\} + i * \text{Im}\{\rho_{10}^1\}}{\rho_{11}^1} \end{pmatrix} \\
\rho^2 &= \begin{pmatrix} \rho_{11}^2 & \frac{\text{Re}\{\rho_{10}^2\} + i * \text{Im}\{\rho_{10}^2\}}{0} & \frac{i * \text{Im}\{\rho_{1-1}^2\}}{\text{Re}\{\rho_{10}^2\} - i * \text{Im}\{\rho_{10}^2\}} \\ \cdot & \cdot & -\rho_{11}^2 \end{pmatrix} \\
\rho^3 &= \begin{pmatrix} \rho_{11}^3 & \frac{\text{Re}\{\rho_{10}^3\} + i * \text{Im}\{\rho_{10}^3\}}{0} & \frac{i * \text{Im}\{\rho_{1-1}^3\}}{\text{Re}\{\rho_{10}^3\} - i * \text{Im}\{\rho_{10}^3\}} \\ \cdot & \cdot & -\rho_{11}^3 \end{pmatrix}
\end{aligned}$$

RESULTS

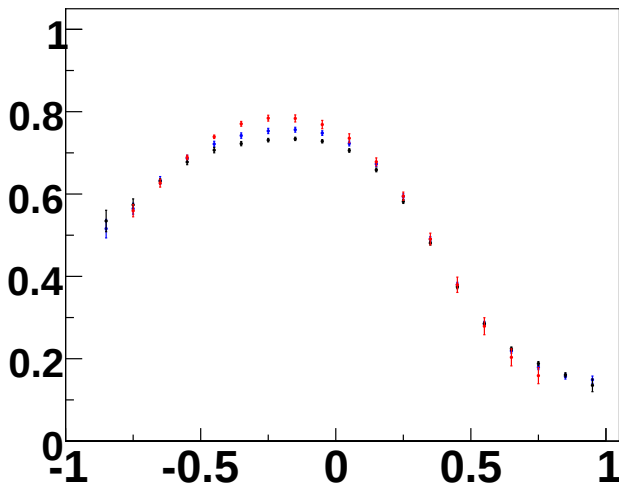
- Results presented come from *mother* fit
 - Amplitudes from $J=1/2$ up to $J=11/2$, both parities
- Previous experiment, g11a
- The three ρ^0 elements from g8b are presented compared to the results from g11a
- Then the ρ^1 and ρ^2 elements from g8b and the ρ^3 elements from g1c will be presented
- Errors are calculated using the bootstrap method
- The g8b data is in black, the g11a data is in red, and the g1c data is in blue when presented together

ρ_{00}^0 IN G8B


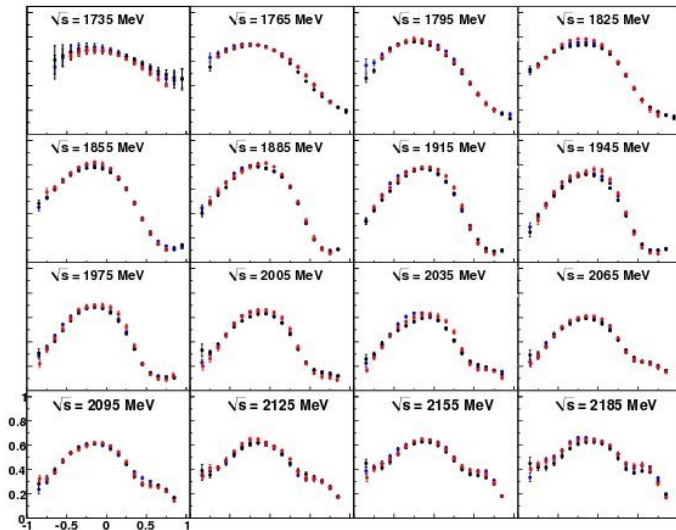
ρ_{00}^0 IN $\sqrt{s} = 1825$ MEV BIN



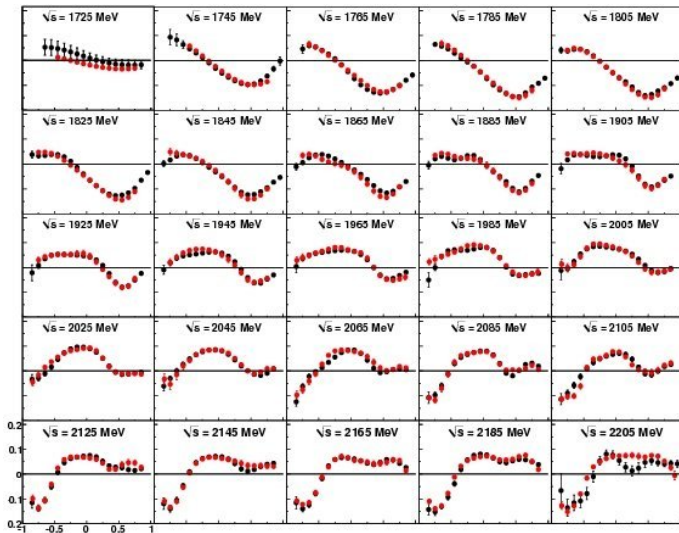
ρ_{00}^0 FROM G8B (BLACK), G1C (BLUE), G11A (RED)

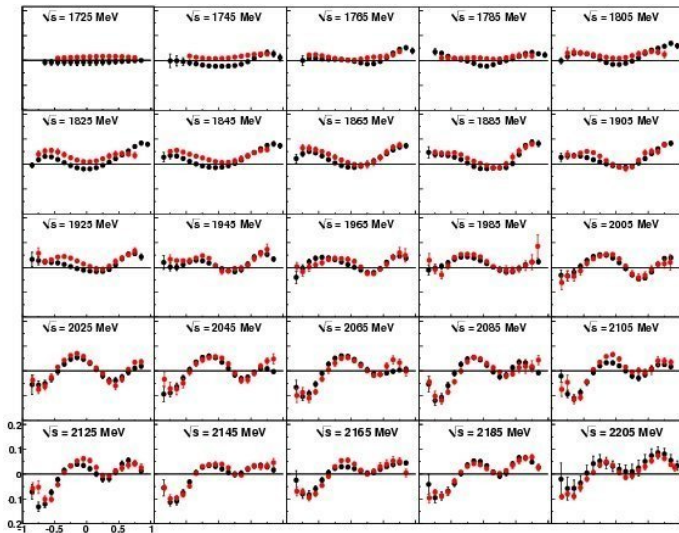


ρ_{00}^0 FROM G8B (BLACK), G1C (BLUE), G11A (RED)

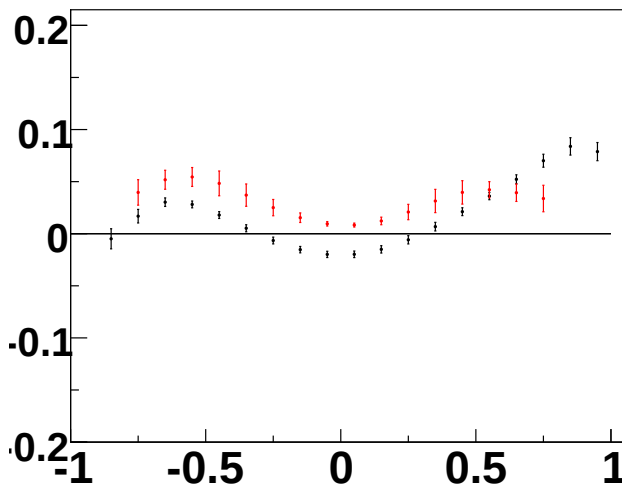


$\text{Re}(\rho_{10}^0)$ IN G8B

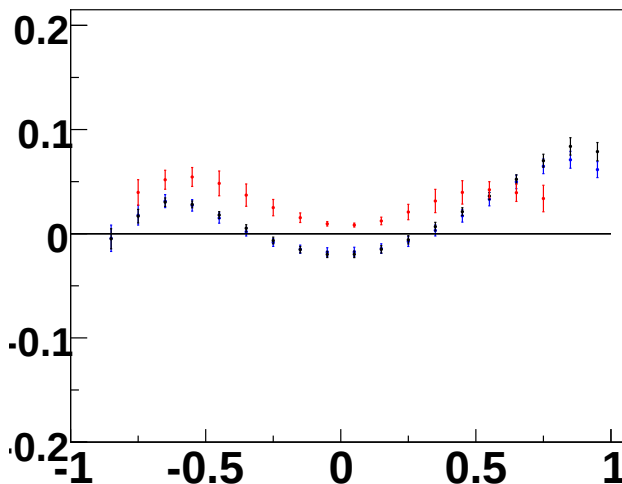


ρ_{1-1}^0 IN G8B

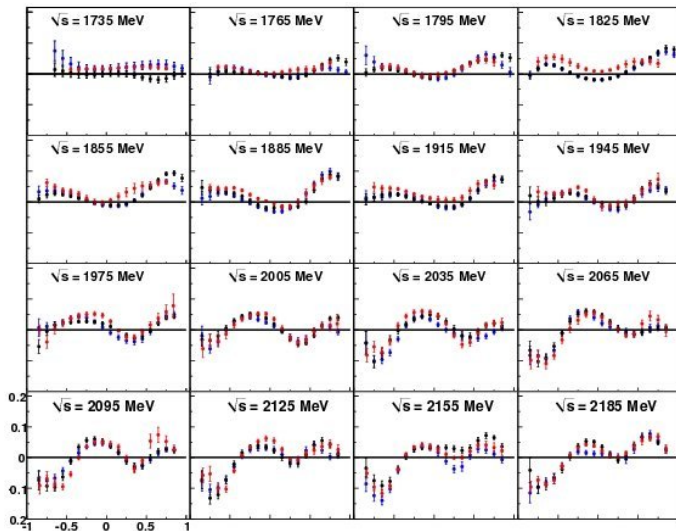
ρ_{1-1}^0 IN $\sqrt{s} = 1825$ MEV BIN

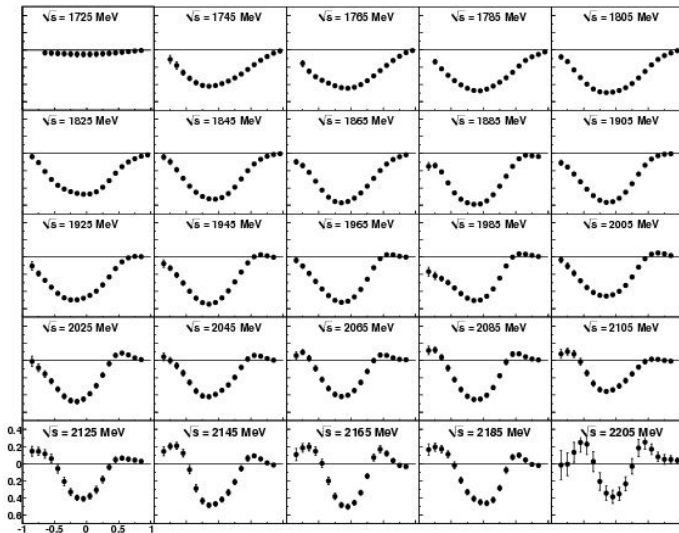


ρ_{1-1}^0 FROM G8B (BLACK), G1C (BLUE), G11A (RED)

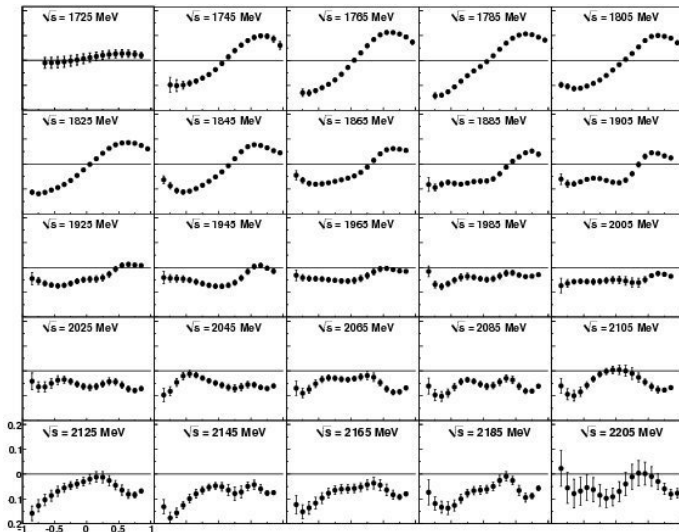


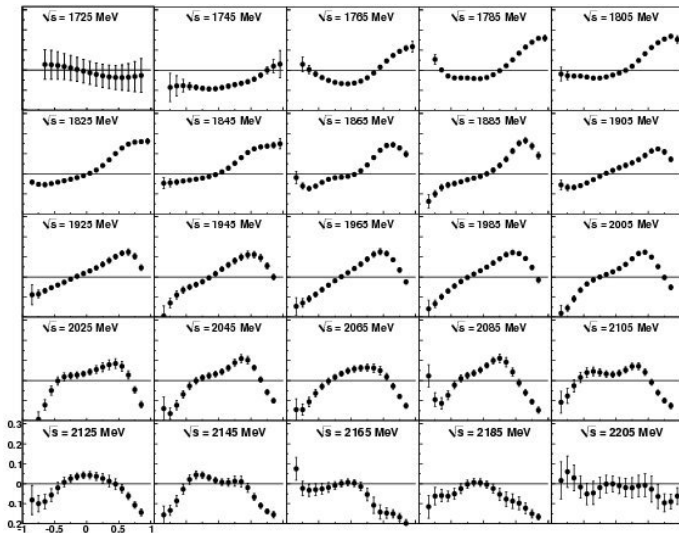
ρ_{1-1}^0 FROM G8B (BLACK), G1C (BLUE), G11A (RED)

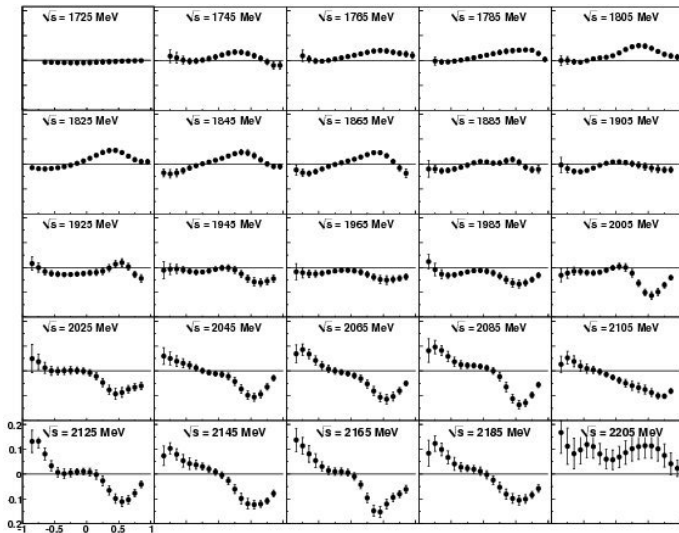


ρ_{00}^1 IN G8B


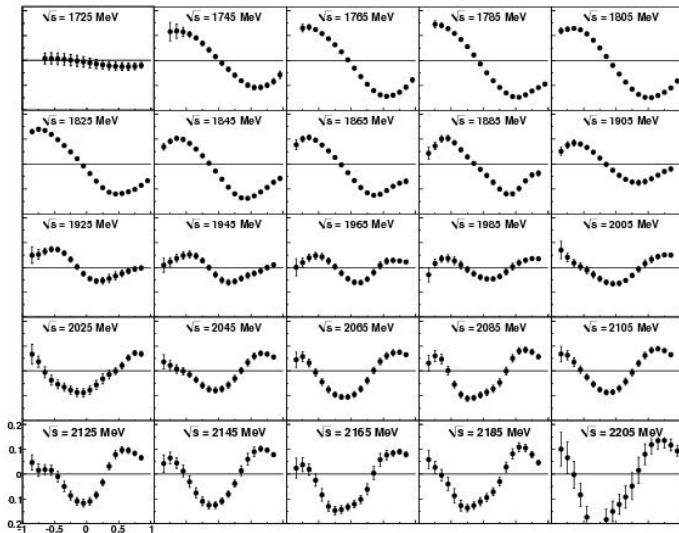
$\text{Re}(\rho_{10}^1)$ IN G8B



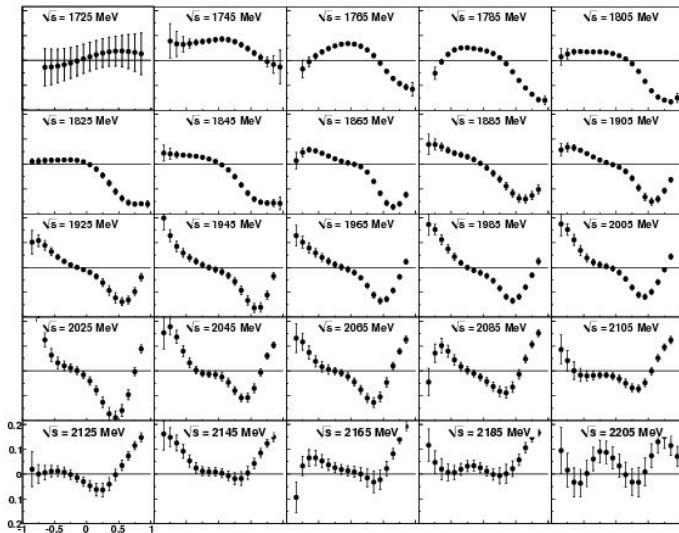
ρ_{1-1}^1 IN G8B


ρ_{11}^1 IN G8B

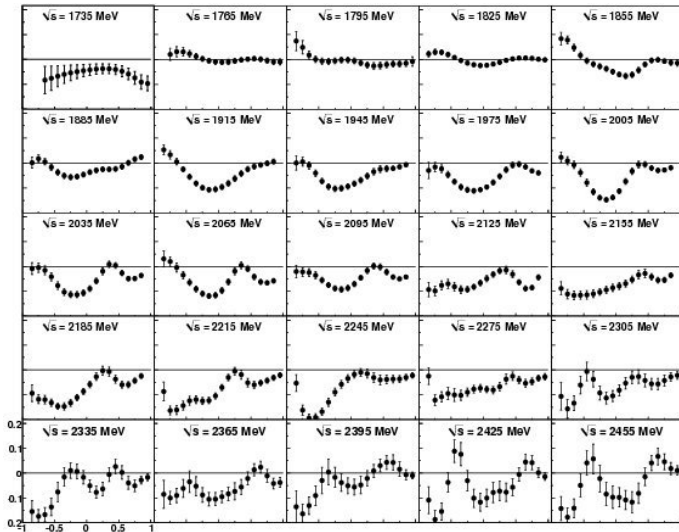
$\text{Im}(\rho_{10}^2)$ IN G8B



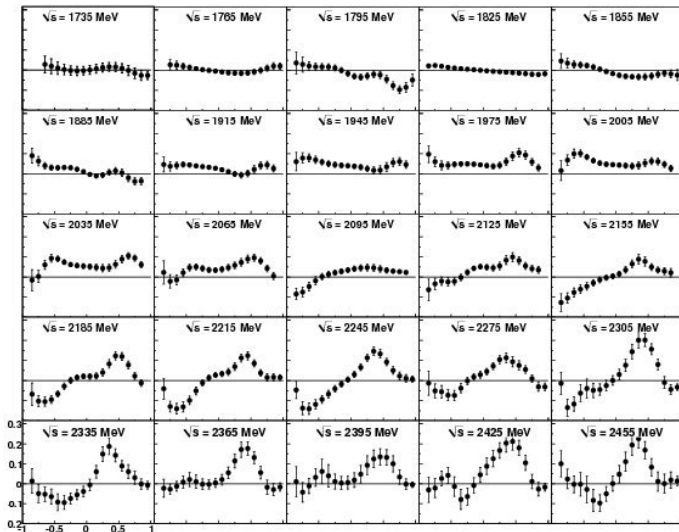
$\text{Im}(\rho_{1-1}^2)$ IN G8B



$\text{Im}(\rho_{10}^3)$ IN G1C



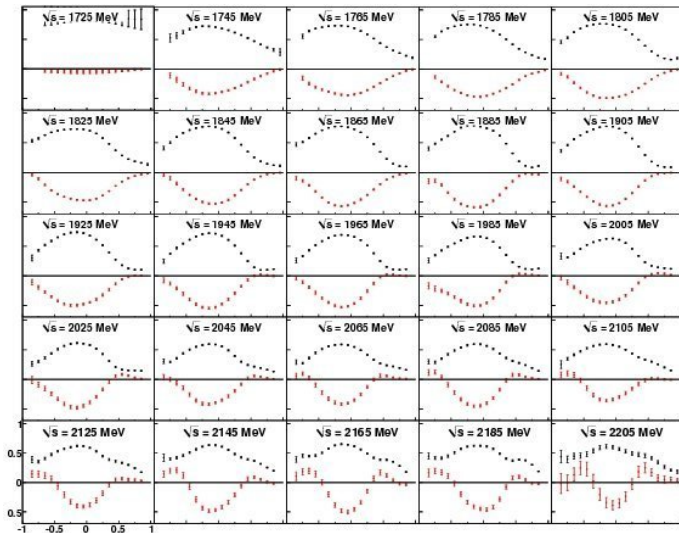
$\text{Im}(\rho_{1-1}^3)$ IN G1C



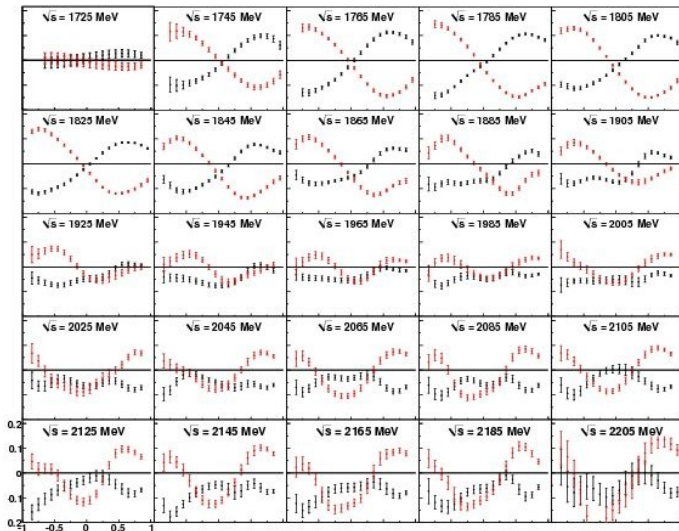
SYMMETRIES

- There are a few symmetries that are present among the new SDMEs
- For almost the entire energy range under study the ρ_{00}^1 element mirrors the ρ_{00}^0 element
- Below 1825 MeV, $\text{Re}(\rho_{10}^1)$ and $\text{Im}(\rho_{10}^2)$ mirror each other's movements
- At almost all energies, ρ_{1-1}^1 and $\text{Im}(\rho_{1-1}^2)$ elements are near exact mirrors

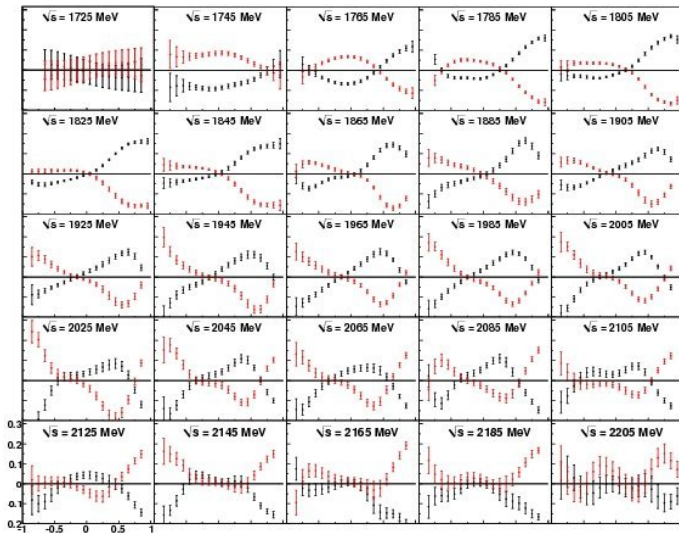
ρ_{00}^0 (BLACK) COMPARED TO ρ_{00}^1 (RED)



$\text{Re}(\rho_{10}^1)$ (BLACK) COMPARED TO $\text{Im}(\rho_{10}^2)$ (RED)



ρ_{1-1}^1 (BLACK) COMPARED TO $\text{Im}(\rho_{1-1}^2)$ (RED)



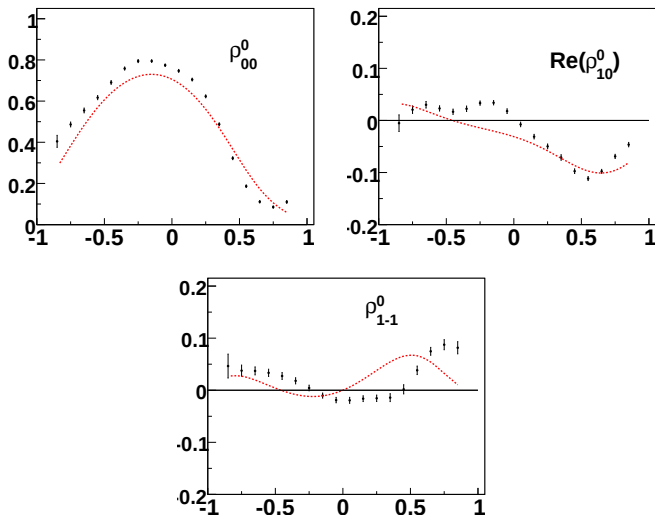
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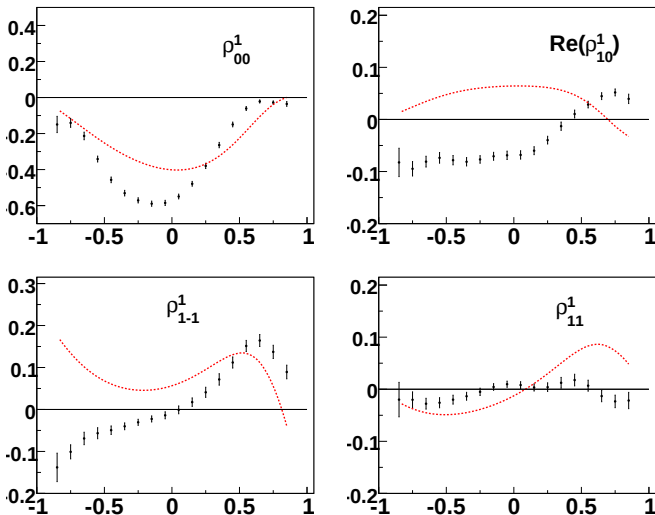
PWA IN G8B

- Our PWA fits are computed with a limited number of s-wave amplitudes along with t-channel amplitudes constructed and parameters locked to the Oh, Titov and Lee model for non-resonant channels
- All combinations of two s-waves (up to $J = 11/2$) with the t-channel are run through the same fitter used for the mother fit
- Determine best fits by comparing final log likelihood values and comparing observables, SDMEs
- In g11a, the $3/2^-$, $5/2^+$ combination was the best fit from 1720-2000 MeV, and was able to reproduce many aspects of the ρ^0 elements
- The added SDMEs prove that more resonances are required

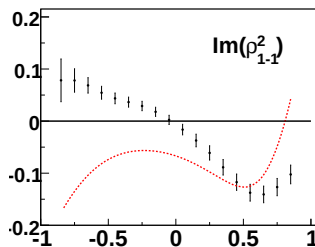
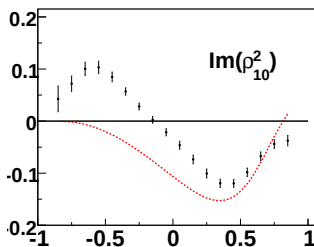
ρ^0 FROM G8B 3/2-, 5/2+ FIT FOR $\sqrt{s} = 1885$ MEV



ρ^1 FROM G8B 3/2-, 5/2+ FOR $\sqrt{s} = 1885$ MEV



ρ^2 FROM G8B 3/2-, 5/2+ FOR $\sqrt{s} = 1885$ MEV



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SUMMARY

- We have modified our fitting code to include photon polarization
- Measurements of the unpolarized SDMEs agree well with what was seen in g11a
- First measurements have been made of the ρ^{1-3} SDMEs for ω photoproduction over a wide range of angles and energies
- These additional elements have aided our search for the resonances important in ω production, making it clear that there is more going on than was seen in the unpolarized fits
- Adding in target polarization will increase the analyzing power even more

BACKUP SLIDES

- BACKUP SLIDES

BRIEF DENSITY MATRIX REMINDER

- Density matrices represent particles that can be in multiple states
- If the density matrix for a particle is known then all QM observables can be calculated
- For a particle with n states, each having wave function $|\psi_i\rangle$, the density matrix can be constructed as

$$\rho = \sum_{i,i'}^n a_{ii'} |\psi_{i'}\rangle \langle \psi_i| \quad (2)$$

- Diagonal elements represent the probability that the particle is in state $|\psi_i\rangle$
- Off-diagonal elements, $\rho_{ii'}$, represent the probability of a transition from state $|\psi_i\rangle$ to state $|\psi_{i'}\rangle$
- An unpolarized particle's density matrix is the identity matrix
- For this talk the density matrix will always be in the spin space

DETERMINING ρ_γ

- The density matrix for a photon can be constructed by knowing the photon has two spin states
- These are denoted as $|m_\gamma = + \rangle$ and $|m_\gamma = - \rangle$
- Now ρ_γ can be written as a linear combination of the identity matrix and the Pauli matrices dotted into the polarization vector

$$\rho_\gamma = \frac{1}{2}\mathcal{I} + \frac{1}{2}\vec{P}_\gamma\vec{\sigma} \quad (3)$$

$$\vec{P} = (-\eta_L \cos(2\alpha), -\eta_L \sin(2\alpha), \eta_c) \quad (4)$$

- $\eta_{c/L}$ are the polarization values for the circularly/linearly polarized photons, $-1 \leq \eta_c \leq 1$, $0 \leq \eta_L \leq 1$
- Generically the photon density matrix is written

$$\rho_\gamma = \frac{1}{2} \begin{pmatrix} (1 + \eta_c) & -\eta_L e^{-2i\alpha} \\ -\eta_L e^{2i\alpha} & (1 - \eta_c) \end{pmatrix} \quad (5)$$

DECOMPOSITION OF ρ_V

- The density matrix for a photoproduced vector meson with an unpolarized target is related to the density matrix of the photon by:

$$\rho_V = J\rho_\gamma J^\dagger \quad (6)$$

- J can be taken to be a matrix of the production amplitudes calculated in the center of mass frame
- Since ρ_γ can be decomposed so can ρ_V

$$\rho_V = \rho_V^0 + \sum_{i=1}^3 P_\gamma^i \rho_V^i \quad (7)$$

$$\rho_V^i = J\rho_\gamma^i J^\dagger \quad (8)$$

- No measurements of the $\rho^{1,2,3}$ elements have previously been performed for the ω meson

EQUATIONS FOR ρ_V

- The equations for the SDMEs are then as follows:

$$\rho_{m_V m_{V'}}^0 = \frac{1}{2N} \sum_{m_\gamma m_i m_f} A_{m_\gamma, m_i, m_f, m_V} * A_{m_\gamma, m_i, m_f, m_{V'}}^\dagger \quad (9)$$

$$\rho_{m_V m_{V'}}^1 = \frac{1}{2N} \sum_{m_\gamma m_i m_f} A_{m_\gamma, m_i, m_f, m_V} * A_{-m_\gamma, m_i, m_f, m_{V'}}^\dagger \quad (10)$$

$$\rho_{m_V m_{V'}}^2 = \frac{i}{2N} \sum_{m_\gamma m_i m_f} (-m_\gamma) A_{m_\gamma, m_i, m_f, m_V} * A_{-m_\gamma, m_i, m_f, m_{V'}}^\dagger \quad (11)$$

$$\rho_{m_V m_{V'}}^3 = \frac{1}{2N} \sum_{m_\gamma m_i m_f} m_\gamma A_{m_\gamma, m_i, m_f, m_V} * A_{m_\gamma, m_i, m_f, m_{V'}}^\dagger \quad (12)$$

MEASURABLE ELEMENTS

$$\begin{aligned}
 \rho^0 &= \begin{pmatrix} \frac{1}{2}(1 - \rho_{00}^0) & \frac{\text{Re}\{\rho_{10}^0\} + i * \text{Im}\{\rho_{10}^0\}}{\rho_{00}^0} & \frac{\text{Re}\{\rho_{1-1}^0\}}{\frac{1}{2}(1 - \rho_{00}^0)} \\ & & \frac{-\text{Re}\{\rho_{10}^0\} + i * \text{Im}\{\rho_{10}^0\}}{\frac{1}{2}(1 - \rho_{00}^0)} \end{pmatrix} \\
 \rho^1 &= \begin{pmatrix} \rho_{11}^1 & \frac{\text{Re}\{\rho_{10}^1\} + i * \text{Im}\{\rho_{10}^1\}}{\rho_{00}^1} & \frac{\text{Re}\{\rho_{1-1}^1\}}{\rho_{11}^1} \\ & & \frac{-\text{Re}\{\rho_{10}^1\} + i * \text{Im}\{\rho_{10}^1\}}{\rho_{11}^1} \end{pmatrix} \\
 \rho^2 &= \begin{pmatrix} \rho_{11}^2 & \frac{\text{Re}\{\rho_{10}^2\} + i * \text{Im}\{\rho_{10}^2\}}{0} & \frac{i * \text{Im}\{\rho_{1-1}^2\}}{\text{Re}\{\rho_{10}^2\} - i * \text{Im}\{\rho_{10}^2\}} \\ & & \frac{-\rho_{11}^2}{\text{Re}\{\rho_{10}^2\} - i * \text{Im}\{\rho_{10}^2\}} \end{pmatrix} \\
 \rho^3 &= \begin{pmatrix} \rho_{11}^3 & \frac{\text{Re}\{\rho_{10}^3\} + i * \text{Im}\{\rho_{10}^3\}}{0} & \frac{i * \text{Im}\{\rho_{1-1}^3\}}{\text{Re}\{\rho_{10}^3\} - i * \text{Im}\{\rho_{10}^3\}} \\ & & \frac{-\rho_{11}^3}{\text{Re}\{\rho_{10}^3\} - i * \text{Im}\{\rho_{10}^3\}} \end{pmatrix}
 \end{aligned}$$

PARTIAL WAVE FITS

- The method used for our partial wave analysis is an event-based extended maximum likelihood fit
- No binning is done to the data other than in narrow $\sqrt{s}$ bins
- The likelihood function, $\mathcal{L}$, is dependent upon a set of parameters acting as weights for the amplitudes
- For all data the function we need to minimize is

$$-\ln \mathcal{L} = - \sum_i^{N_{events}} \ln |\mathcal{M}(\vec{x}, X_i)|^2 + \frac{\mathcal{S}(s)}{N_{raw}} \sum_i^{N_{acc}} |\mathcal{M}(\vec{x}, X_i)|^2 + const. \quad (14)$$

- $\mathcal{M}$ is the Lorentz invariant transition amplitude taking the initial state γp to the final state $p\pi^+\pi^-\pi^0$
- $\mathcal{M}$ can be interpreted as the non-normalized cross section

DETERMINING THE TRANSITION AMPLITUDE

- $\mathcal{M}$ is determined from the following equation

$$|\mathcal{M}|^2 = \text{Tr}[J(\rho_\gamma \otimes \rho_i)J^\dagger] \quad (15)$$

- J in the above equation is a 2×4 matrix of the production amplitudes

$$J = \begin{pmatrix} A_{+++} & A_{+-+} & A_{-++} & A_{--+} \\ A_{++-} & A_{+--} & A_{-+-} & A_{---} \end{pmatrix} \quad (16)$$

- The direct product between ρ^γ and ρ^i results in a 4×4 matrix which represents the initial space of the reaction
- In the unpolarized case both ρ_γ and ρ_i are the identity matrix and so M becomes:

$$|\mathcal{M}|^2 = \text{Tr}[JJ^\dagger] = \sum_{m_\gamma, m_i, m_f} |A_{m_\gamma, m_i, m_f}|^2 \quad (17)$$

CIRCULAR POLARIZATION

- Recall that the photon density matrix is written

$$\rho_\gamma = \frac{1}{2} \begin{pmatrix} (1 + \eta_c) & -\eta_L e^{-2i\alpha} \\ -\eta_L e^{2i\alpha} & (1 - \eta_c) \end{pmatrix} \quad (18)$$

- For the case of circular polarization this leads to

$$|\mathcal{M}|^2 = \sum_{m_i, m_f} ((1 + \eta_c) |A_{+, m_i, m_f}|^2 + (1 - \eta_c) |A_{-, m_i, m_f}|^2) \quad (19)$$

- Note that η_c ranges from -1 to 1, being negative/positive when the helicity is measured to be left/right

LINEAR POLARIZATION

- In the case of linear polarization $\mathcal{M}$ is the following

$$|\mathcal{M}|^2 = \sum_{m_i, m_f} (|A_{+,m_i,m_f}|^2 + |A_{-,m_i,m_f}|^2 - \eta_L (e^{-2i\alpha} A_{+,m_i,m_f} A_{-,m_i,m_f}^\dagger + e^{2i\alpha} A_{-,m_i,m_f} A_{+,m_i,m_f}^\dagger)) \quad (20)$$

- Clearly there is an unpolarized part and a polarized part,
- The polarized part includes a mixing of amplitude types
- The polarized part is separated into a sum of conjugates
- Thus the polarized part is completely real

MONTÉ CARLO

- The same $\mathcal{M}$ function must be used for the monte carlo data as for the measured data to properly normalize the data
- MC data is thrown only as 4-vectors to equally populate the allowed phase space
- This requires each MC event be assigned a polarization
- For circularly polarized experiments each MC event is assigned a polarization according to the Maximon and Olson relationship
- For linearly polarized data η_L depends on the instantaneous coherent edge, which does not exist in the MC
- The average polarization for the data in a given bin is used as η_L for all MC events in that bin
- This approximation should be valid as long as the polarization in a bin is tightly bound, which is true